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Sc₂Ga₂CuO₇: A possible Quantum spin liquid near the percolation threshold

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Abstract

Sc₂Ga₂CuO₇ (SGCO) crystallizes in a hexagonal structure (space group: $P6_3/mmc$), which can be seen as an alternating stacking of single and double triangular layers. Combining neutron, x-ray, and resonant x-ray diffraction we establish that the single triangular layers are mainly populated by non-magnetic Ga³⁺ ions (85% Ga and 15% Cu), while the bi-layers have comparable population of Cu²⁺ and Ga³⁺ ions (43% Cu and 57% Ga). Our susceptibility measurements in the temperature range 1.8 - 400 K give no indication of any spin-freezing or magnetic long-range order (LRO). We infer an effective paramagnetic moment $\mu_{eff} = 1.79 \pm 0.09 \mu_B$ and a Curie-Weiss temperature θ_{CW} of about -44 K, suggesting antiferromagnetic interactions between the Cu²⁺ ($S = 1/2$) ions. Low-temperature neutron powder diffraction data showed no evidence for LRO down to 1.5 K. In our specific heat data as well, no anomalies were found down to 0.35 K, in the field range 0-140 kOe. The magnetic specific heat, C_m , exhibits a broad maximum at around 2.5 K followed by a nearly power law $C_m \propto T^\alpha$ behavior at lower temperatures, with α increasing from 0.3 to 1.9 as a function of field for fields upto 90 kOe and then remaining at 1.9 for fields upto 140 kOe. Our results point to a disordered ground state in SGCO.

PACS numbers: 75.10.Jm, 75.10.Kt, 75.40.Cx

Introduction: Geometrically frustrated spin systems are full of surprises and continue to draw attention because of their tendency to host novel ground states [1]. In particular, triangular lattice based geometrically frustrated Mott insulators have gained wide interest because their ground states were envisaged to be based on a Resonating Valence Bond (RVB) picture [2]. Anderson's RVB proposal [2] pertained to the two dimensional (2D) edge-shared triangular lattice which, however, has a 120° ordered ground state [3–6]. This, in particular, triggered the search for the RVB state (also called the quantum spin liquid QSL state [1]) in geometries such as triangular (anisotropic), Kagomé (2D), hyperkagomé (three dimensional 3D), and pyrochlore (3D). Finally, a QSL state was realized notably in the 2D triangular system κ -(BEDT-TTF)₂Cu₂(CN)₃[7], the Kagomé system ZnCu₃(OH)₆Cl₂ [8–12], and the hyperkagomé system Na₄Ir₃O₈ [13, 14]. A frustrated geometry and a low value of spin ($S = 1/2$), which enhances quantum fluctuations, help in stabilizing a QSL state [1]. However, even in the 6H-B and 3C phases of Ba₃NiSb₂O₉ (Ni²⁺, $S = 1$) [15], which have 2D edge-shared triangular and 3D edge-shared tetrahedral lattices, respectively, a QSL

state has been suggested. Also, the realization of a QSL state for Ba₃IrTi₂O₉ [16], containing a diluted triangular lattice, and Ba₃YIr₂O₉ (high pressure cubic phase) [17], possibly suggests the importance of further neighbor interaction and/or deviations from the Heisenberg model. Recent experimental/theoretical results suggest that disorder might even drive the QSL state [18, 19]. The unconventional nature of its elementary excitations, which result from a chargeless sector of spin-1/2 fermions (commonly known as spinons), also drew interest from theorists and experimentalists [1, 20, 21]. Spinons are believed to form a Fermi surface in such Mott insulators and a non-vanishing Sommerfeld coefficient (γ) appears to be a generic feature for most of the previously discussed QSL [7, 13, 15, 17].

We have been exploring a variety of spin systems with the objective of finding new QSL especially investigating triangular lattices. Herein, we introduce a Cu²⁺ ($S = 1/2$) based potential QSL system Sc₂Ga₂CuO₇ (SGCO). This system was first reported by Kimizuka *et al.* [22] and the structure type was identified as similar to Yb₂Fe₃O₇ [23]. However, no other data have been reported up to now. Here we report a thorough investigation of the structure and magnetic properties of SGCO by synchrotron x-ray diffraction (xrd), neutron diffraction (ND), susceptibility, and specific heat measurements. In the Yb₂Fe₃O₇ structure as applied to SGCO, the 4f sites

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(forming triangular bi-layers) are expected to be occupied by Ga and 2b sites (forming single triangular layers) by Cu (see Fig. 1). However, we found a large deviation from this expectation. The Ga and Cu occupancies are not easy to obtain due to their similar scattering lengths for neutron as well as similar atomic scattering factors for xrd. From the xrd (synchrotron) data, where the x-ray energy was tuned to be near the K-absorption edge of Cu, we could reliably estimate the 4f and 2b site occupancies by Ga and Cu. Combined with our magnetization and heat capacity data, this allows us to suggest that the magnetic lattice of SGCO comprises of (i) triangular bi-planes, (double layers of triangular bi-pyramids), of $S = 1/2$ Cu which are nearly 50% diluted by Ga but give rise to spin liquid behavior and (ii) some uncorrelated Cu located at a different site. For magnetic fields higher than 90 kOe the magnetic heat capacity exhibits a power law behavior with an exponent close to 2 as in many QSL systems [13, 15].

Sample preparation and experimental details: Several batches of polycrystalline SGCO were synthesized by a conventional solid-state reaction route (see Supplementary Material [24]). Xrd data were collected at 300 K using a PANalytical diffractometer using Cu-K α radiation ($\lambda = 1.54182$ Å). Synchrotron xrd data were measured at room temperature at the Materials Sciences Beamline [25] of the Swiss Light Source (SLS), with the wavelength 0.6204 Å, using the Mythen-II detector. Data were also taken at $\lambda = 1.38455$ Å ($E = 8.9548$ keV) which is just below the K-absorption edge of Cu ($E = 8.9789$ keV). Silicon powder was added to the substance in order to substantially reduce the x-ray absorption in the sample. The ND measurements were carried out with the HRPT diffractometer [26] at the SINQ neutron source ($\lambda = 1.49$ Å) of Paul Scherrer Institut at 300 K and 1.5 K using a standard orange cryostat. Magnetization M measurements were done using a Quantum Design SQUID VSM in the temperature T range 1.8 - 400 K and in magnetic fields H upto 70 kOe. The ac susceptibility measurements were performed on a dilution refrigerator (0.3-7 K) and on a Quantum Design SQUID VSM in the T range 2 - 30 K [24]. The heat capacity measurements were done in the T -range 0.35 - 295 K, using a Quantum design PPMS.

Structure and magnetic model: The powder xrd and ND patterns of SGCO could be indexed within the space group $P6_3/mmc$ (194) and correspond to the $\text{Yb}_2\text{Fe}_3\text{O}_7$ structure previously reported by Kimizuka *et al.* [22, 23]. Our lab xrd data (not shown) did not show any impurity peaks, however in the much higher statistics synchrotron data we found Sc_2O_3 (~ 1.2 wt.%) and CuGa_2O_4 (~ 0.5 wt.%) impurities. A three phase Rietveld refinement using FullProf [27] was done on our synchrotron data to obtain the lattice constants and the absolute amount of phases. The refined synchrotron data with ($\lambda = 0.62$ Å) and the extracted atomic positions for SGCO are summarized in the Supplementary Material [24]. The obtained lattice constants are $a = b = 3.30395(3)$ Å and

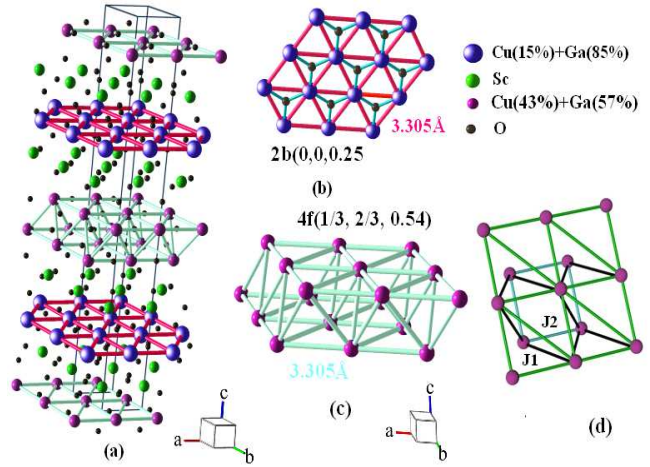


Figure 1: (Color online) (a) The unit cell of SGCO is shown. (b) Edge-shared triangular plane of the 2b (0, 0, 1/4) sites is shown. (c) Triangular bi-planes from the 4f site (1/3, 2/3, 0.54) are shown. (d) an alternative representation of (c): to maintain clarity, not all atoms are shown). The 2b and 4f sites are shared by Cu and Ga (see legend and text).

$c = 28.1116(3)$ Å, similar to those reported by Kimizuka *et al.* [22].

Since Cu and Ga have similar scattering lengths, both for x-rays and for neutrons, possible site sharing between the two is not easily addressed by analyzing the diffraction data. For instance, for x-rays ($\lambda = 0.62$ Å) the atomic scattering factors for Ga and Cu are different by only 7%. However, if one tunes the x-ray energy near the K-absorption edge of Cu, the difference in scattering factors for Ga and Cu can be much more. In our case ($\lambda = 1.38455$ Å), the scattering factors for Ga and Cu are different by 25%. Xrd pattern under these conditions is shown in Fig. 2. The obtained lattice constants are $a = b = 3.3045(2)$ Å, $c = 28.1129(1)$ Å (see Supplementary Material [24] for details). We find that the 2b sites (0, 0, 1/4) contain 85% non-magnetic Ga^{3+} and 15% Cu^{2+} . The 4f sites (1/3, 2/3, z) contain 57% Ga^{3+} and 43% Cu^{2+} ions. As shown in Fig. 1 (b) the edge-shared single-triangular planes at the 2b sites (0, 0, 1/4), along with the neighboring oxygens atoms make single layers of corner-sharing triangular bi-pyramids (see Supplementary Material [24]). On the other hand, the 4f sites (1/3, 2/3, 0.54) form triangular bi-planes (see Fig. 1 (c)) or rather double layers of triangular bi-pyramids when the oxygens are included. In a bi-plane (4f sites), a triangular layer is shifted with respect to the other such that the vertices of one layer are at the centroids of alternate triangles of the other layer. This is topologically equivalent to a honeycomb lattice with nearest ($J1$) and next-nearest ($J2$) neighbor coupling and based on exchange paths it is likely that $J2 > J1$, see Fig. 1 (d).

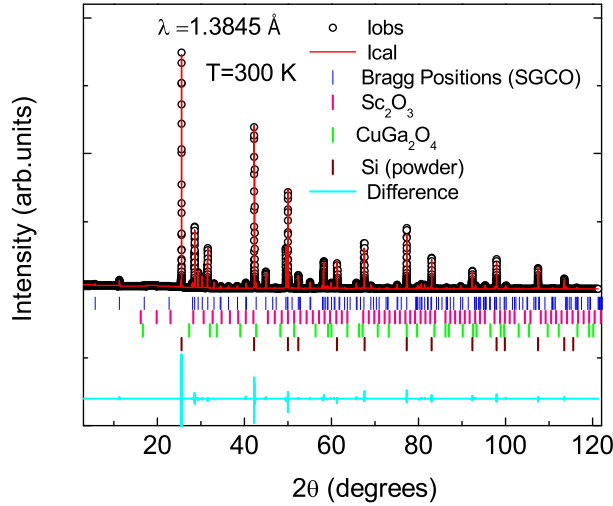


Figure 2: (Color online) Resonant xrd (SLS) data ($\lambda = 1.38455 \text{ \AA}$) for SGCO at 300 K refined with the space group $P6_3/mmc$. Iobs and Ical represent the experimental and Rietveld refined intensities, respectively. The vertical blue, pink, green and brown bars depict the Bragg positions for SGCO, Sc_2O_3 , CuGa_2O_4 and Si (internal standard), respectively, whereas flat cyan line shows Iobs- Ical.

The preference for Ga for the 2b sites is supported by bond-valence sum (BVS) calculations. The BVS for Ga^{3+} is 2.91 on 2b sites and 2.69 on 4f sites, making 2b the preferred site for Ga^{3+} . Likewise the BVS for Cu is 2.54 on 2b sites and 2.35 on 4f sites, giving a slight preference for Cu^{2+} to occupy 4f sites, in agreement with the results from the structural refinements.

The dc susceptibility ($\chi = \frac{M}{H}$) of SGCO varies in a Curie-Weiss manner $\chi = \chi_0 + C/(T - \theta_{CW})$ down to 100 K, where χ_0 ($-4.451 \times 10^{-5} \text{ cm}^3/\text{mol}$), $C = 0.41 \text{ cm}^3 \text{ K/mol}$, and $\theta_{CW} = -44 \text{ K}$ denote the T -independent χ , the Curie constant, and the Curie-Weiss temperature, respectively. The negative θ_{CW} suggests antiferromagnetic correlations and the inferred effective moment $\mu_{eff} \approx \sqrt{8C} = 1.79 \pm 0.09 \mu_B$ is close to that for an $S = 1/2$ moment. Measurements performed in a low field (25 Oe) and down to 2 K do not exhibit any anomaly or bifurcation between zero field cooled (ZFC) and field cooled (FC) data (inset of Fig. 3). AC χ measurements in the T -range 0.3-30 K do not show any anomaly or frequency dependence (see the Supplemental material [24]). This suggests the absence of LRO or any spin freezing. It is worth mentioning that the ND measurements carried out at 1.5 K did not show any signature of magnetic Bragg peaks, setting an upper limit of $0.5 \mu_B$ for the ordered moment in case of LRO. Further, ^{71}Ga NMR shift data [28] on SGCO indicate a leveling off of χ below about 50 K and the absence of LRO. While further evidence is needed to conclusively establish QSL behav-

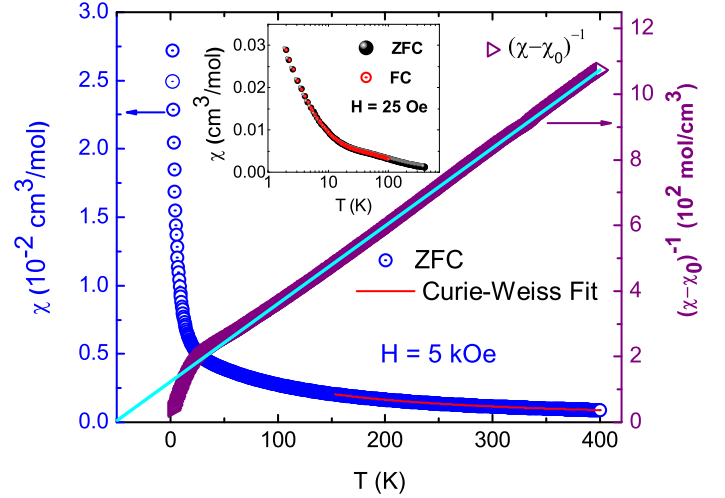


Figure 3: (Color online) The left y -axis shows the T -dependence of χ (blue open circles) measured in $H = 5 \text{ kOe}$ and the right y -axis shows the inverse χ plot (purple open triangles) free from the T -independent χ . The Curie-Weiss fit is shown in the T -range 150 K - 400 K with a red solid line and the inset depicts the absence of any ZFC/FC bifurcation in $\chi(T)$ in $H = 25 \text{ Oe}$.

ior in SGCO, the essential features of $\chi(T)$ in SGCO are as in other QSL materials.

To estimate the fraction of paramagnetic spins in SGCO, we have made use of the data from magnetic isotherms $M(H)$ at low- T (1.8 - 4.5 K) since the Cu at the 2b sites is expected to show paramagnetic Curie-like behavior while the contribution from the possibly correlated triangular bi-planes might be much lower. Our analysis (see the Supplemental material [24]) of the $M(H)$ data is consistent with about 12% of paramagnetic Cu^{2+} ($S = 1/2$) spins which is not far from the value of 15% Cu at the 2b sites obtained from resonant xrd data. In $\text{In}_2\text{Ga}_2\text{CuO}_7$, structurally similar to SGCO, Taetz *et al.* [29] obtained approximately 10% of paramagnetic $S = 1/2$ impurities from a similar analysis. Given the site occupancies obtained from resonant xrd results on SGCO, the magnetic lattice (bi-layers from the atoms at 4f positions (1/3, 2/3, 0.54)) is more than 50% diluted. While this is beyond the percolation threshold of a 2D triangular lattice, for the bi-layer configuration (or the honeycomb lattice as mentioned before) here, the magnetic connectivity might still be maintained.

Based on our experiments, we suggest that SGCO appears to consist of (i) 10-15% of the 2b sites having $S = 1/2$ paramagnetic moments and (ii) a nearly equal mixture of $S = 1/2 \text{ Cu}^{2+}$ and $S = 0 \text{ Ga}^{3+}$ at the 4f sites which magnetically form the triangular bi-planes. While it could be that the site occupation is correlated, maintaining the magnetic connectivity in the triangular bi-layers, it is surprising that there is no spin-freezing even

after large dilution. One may speculate that the proximity of the site occupation to a percolation threshold may promote long range spin singlets as in an algebraic spin liquid [1].

Heat capacity: To obtain further insight into the low-energy excitations of SGCO, we measured its specific heat $C_p(T)$ (Fig. 4) in the T -range 0.35 - 300 K under various H (0 kOe - 140 kOe). We found no signature of LRO down to 0.35 K. However, below about 15 K the $C_p(T)$ displays a dependence on H which is suggestive of a Schottky anomaly. This Schottky contribution $C_{Schottky}$ most likely arises from the paramagnetic Cu^{2+} spins at the 2b sites. Note that our $M(H)$ data analysis revealed a $\sim 12\%$ contribution from paramagnetic $S = 1/2$ species. We then analyzed $C_p(T)$ as a combination of $C_{Schottky}$ and $C_{lattice}$ (the lattice heat capacity) in addition to a magnetic heat capacity C_m (see Supplemental Material [24]). The C_m (which, we believe, comes from the correlated spins of the triangular bi-planes) is obtained after subtracting $C_{lattice}$ and $C_{Schottky}$ and is shown in Fig. 4 (b).

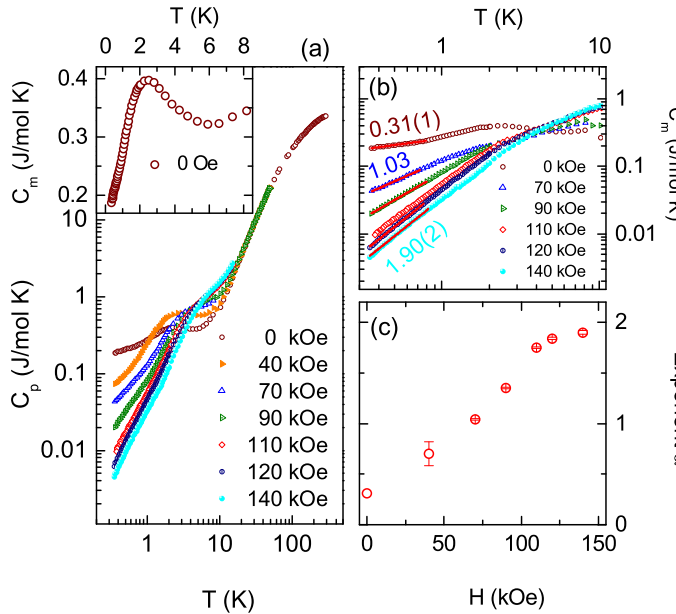


Figure 4: (Color online) (a) The $C_p(T)$ data (log-log scale) for various H (up to 140 kOe) are shown. Inset depicts the appearance of a broad maximum in C_m , in $H = 0$. (b) Power law fits (see text) of C_m are shown as solid lines. (c) Variation of exponent α with H is shown. Note that, for $H > 40$ kOe the size of the error bars is equal to the size of the symbols.

As shown in the inset of Fig. 4 (a), $C_m(T)$ shows a broad maximum (perhaps not related to any phase transition) at around 2.5 K in $H = 0$. The appearance of a broad maximum is common for highly frustrated spin systems and has previously been noticed for NiGa_2S_4 [30], $\text{Na}_4\text{Ir}_3\text{O}_8$ [13], $\text{Ba}_3\text{CuSb}_2\text{O}_9$ [31], and $\text{Ba}_3\text{NiSb}_2\text{O}_9$ [15]. However, its position in T (in comparison to the strength of the exchange coupling) varies from material to mate-

rial.

Finally the low- T C_m data ($T < 1$ K) were fitted to a power-law $C_m = \gamma T^\alpha$ (where γ is a constant), to infer about the magnetic excitations (see Fig. 4 (b)). We found that in SGCO, α increases from 0.3 to 1.9 with increasing H . The error bars for α in Fig. 4 (c) were arrived at by assuming a $\pm 50\%$ uncertainty in $C_{Schottky}$. The value of α is robust and reliable for $H > 40$ kOe in the T -range 0.35-1 K, and attains a value 1.9(2) for $H > 90$ kOe. An exponent close to 2 might be an indication of a QSL and has previously been observed for the hyperkagomé compound $\text{Na}_4\text{Ir}_3\text{O}_8$ [13] as also the 3C phase of $\text{Ba}_3\text{NiSb}_2\text{O}_9$ [15]. In the case of a Kagomé lattice, a theoretical approach (spin-1/2 spinons obeying the Dirac spectrum [32]) leads to a T^2 dependence of specific heat. However, there could be other explanations. Recently, randomness-induced QSL (also called random singlet) has been suggested for organic triangular salts [33] as also for inorganic ones such as herbertsmithite [34] with the Kagomé structure. In herbertsmithite, a Zn/Cu disorder might cause a random Jahn-Teller distortion of the $[\text{Cu}(\text{OH})_6]^{4-}$ giving rise to a random modification of the exchange coupling in the Kagomé layer. For the resulting gapless QSL state, a T -linear C_m is expected. In the SGCO case, a similar Ga/Cu disorder exists which might drive the QSL state. However, in SGCO (in zero field), the power law exponent of C_m is 0.3. This amounts to a divergence of C_m/T at low- T . Such a divergence in $\text{Pr}_2\text{Ir}_2\text{O}_7$ (frustrated moments in a metallic background; different than SGCO) has been seen as an indication of proximity to a quantum critical point QCP [35]. For SGCO, with the increasing $C_m(T)$ exponent (from 0.3 to 1.9) with field, one might speculate that the system moves from a QCP to deeper into the insulating QSL region with field. A cautionary note is that the inferred low-field C_m might be affected by possible interaction between the correlated spins and the orphan spins.

It is worth mentioning that in our C_m data at $H = 140$ kOe, $\gamma \sim 34$ mJ/mol K^{2.9}. A non zero value of γ , in general, indicates the presence of low-energy (likely) gapless excitations for these Mott insulators at low- T . While the reason for the field-induced suppression of the C_m (suggesting a suppression of magnetic excitations) is not clear at this point, it could arise from a freezing out of any interaction between the orphan spins (Cu^{2+} in the 2b sites) and the triangular bi-layers. The estimated entropy change ΔS (see Supplemental Material [24]) by integrating the C_m/T versus T data (in zero field) yields 1.2 J/mol K, which is nearly 20% of that expected for a $S = 1/2$ moment. This value will be even smaller when the data at the highest field are considered. The significantly smaller ΔS is suggestive of a large residual entropy at low temperatures, further suggesting a QSL ground state in SGCO.

Summary: Using the results obtained from various experimental probes such as xrd, ND, dc/ac $\chi(T)$, $M(H)$, and $C_p(T)$, we have explored the properties of SGCO. Our resonant xrd measurements carried out at the K-

absorption edge of Cu allow us to infer the site occupancies of Cu and Ga at the 2b sites (Cu:Ga = 0.15:0.85) and the 4f sites (Cu:Ga = 0.43:0.57). We suggest that the magnetic lattice can be viewed as a combination of (i) highly depleted triangular bi-layers (or honeycomb layers with nearest as also next-nearest neighbor interactions) giving rise to correlated behavior and (ii) about 15% Cu spins which are paramagnetic. Our ND data down to 1.5 K do not show any signature of LRO/spin freezing and are consistent with the dc/ac $\chi(T)$ measurements. Further, the $C_p(T)$ data indicate absence of any transition down to 0.35 K. They are also indicative of the presence of low-energy excitations and for high fields yield $C_m \propto T^2$ below 1 K. Taken together, the apparent lack of LRO or spin freezing and the existence of low-energy (likely gapless) excitations could be indicative of a QSL ground state. Often QSL candidates with site-disorder have been found to display spin freezing. It is therefore unusual to find the combined lack of order and spin-freezing in a system so heavily diluted as the triangular bi-layers are in this compound. This could be a result of the dilu-

tion approaching a percolation threshold and one may speculate if the unusual QSL behavior could arise close to such thresholds. There is also recent work [19] which proposes disorder driven spin-orbital liquid in such systems. Another possibility is disorder induced bond randomness which can give rise to a random singlet QSL as has been suggested in herbertsmithite [34]. Further low- T magnetization and local probe investigations such as μ SR would be useful to explore the properties of SGCO in greater details.

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Supplemental material for $\text{Sc}_2\text{Ga}_2\text{CuO}_7$: A possible Quantum spin liquid near the percolation threshold

A. Sample preparation

Stoichiometric mixtures of pre-dried CuO (99.995% purity), Ga_2O_3 (99.99% purity), and Sc_2O_3 (99.9% purity) were ground homogeneously in an agate mortar and then pelletized. The pellet was placed in a high density alumina crucible and fired at 950°C for 24 hours in a Carbolite tubular furnace. The pellet was further re-ground, pelletized, and then fired two times at 1250°C for 24 hours each. Several such batches were prepared in this study. The final product was light green in color.

B. X-ray (synchrotron) diffraction and neutron diffraction analysis

Figure 5 depicts the x-ray diffraction pattern obtained for SGCO using synchrotron data with $\lambda = 0.6204 \text{ \AA}$. In the ideal case (no site sharing), the Cu and Ga atoms are expected to form single and double triangular lattices comprising of atoms at 2b (0, 0, 1/4) and 4f (1/3, 2/3, z) sites, respectively. However, because of the similar ionic radii of Cu^{2+} and Ga^{3+} ions, a distribution of both might be expected at the 2b (0, 0, 1/4) and the 4f (1/3, 2/3, z) sites. The atomic coordinates refined from the x-ray (synchrotron: SLS) diffraction data measured with $\lambda = 0.6204 \text{ \AA}$ at 300 K for SGCO are given in Table I. Since Cu ($Z = 29$) and Ga ($Z = 31$) have nearly the same atomic scattering factors it is difficult to estimate with high confidence, their distribution with the present x-ray (synchrotron: $\lambda = 0.6204 \text{ \AA}$) analysis. If the Ga:Cu ratio were left as a free parameter, the best refinement of the synchrotron (SLS) data was obtained with the site 2b (0, 0, 1/4) mostly occupied by Ga^{3+} and the 4f (1/3, 2/3, z) site having both Cu^{2+} and Ga^{3+} ions, which is quite opposite to the isostructural compound $\text{Yb}_2\text{Fe}_3\text{O}_7$ where the divalent Fe^{2+} and the trivalent Fe^{3+} ions sit at 2b (0, 0, 1/4) and 4f (1/3, 2/3, z) sites, respectively. The refinement quality factors described by R_p , R_{exp} , R_{wp} and χ^2 are obtained to be 3.56%, 0.34%, 3.50% and 108, respectively. The local environments of Cu^{2+} ions at 2b/4f site can be best viewed as single layers of corner-sharing triangular bi-pyramids/double layers of triangular bi-pyramids, as seen in Fig. 6. As far as the magnetic lattice is concerned, the latter amounts to a (heavily depleted) honeycomb lattice with the presence of both nearest and next-nearest neighbor interactions.

We then collected x-ray diffraction data near the K absorption edge of Cu to get a more reliable distribution

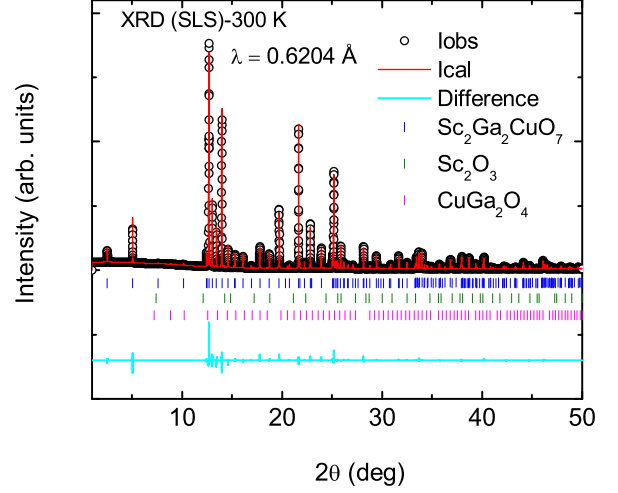


Figure 5: (Color online) X-ray (synchrotron) diffraction data for SGCO recorded at 300 K with wavelength 0.6204 \AA . Iobs and Ical represent the experimental and Rietveld refined intensities, respectively. The vertical blue, pink and green bars depict the Bragg positions for $\text{Sc}_2\text{Ga}_2\text{CuO}_7$, Sc_2O_3 and CuGa_2O_4 , respectively, whereas flat cyan line shows the intensity difference Iobs- Ical.

Table I: Atomic positions obtained after Rietveld refinement of the x-ray (synchrotron:SLS) data at 300 K with $\lambda = 0.6204 \text{ \AA}$.

Atom	site	x	y	z	occ
Sc	4f	1/3	2/3	0.14877(2)	1
Cu	2b	0.0	0.0	1/4	0.252(2)
Ga	2b	0.0	0.0	1/4	0.744(2)
Ga	4f	1/3	2/3	0.54478(1)	0.312(3)
Cu	4f	1/3	2/3	0.54478(1)	0.69(3)
O1	4f	0.0000	0.0000	0.18007(6)	1
O2	4f	1/3	2/3	0.61130(6)	1
O3	4f	1/3	2/3	0.03325(7)	1
O4	2c	1/3	2/3	1/4	1

of Cu and Ga atoms at 2b and 4f sites, as the contrast between the atomic scattering factors of Ga and Cu is higher at this wavelength. From a refinement of our resonant x-ray data with $\lambda = 1.38455 \text{ \AA}$ (refined positions and occupancies are in Table II), we obtain that the 2b sites (0, 0, 1/4) are mostly occupied with non-magnetic Ga^{3+} ions (85% Ga^{3+} and 15% Cu^{2+}), whereas the 4f sites (1/3, 2/3, z), which form a network of double layers of triangular bi-pyramids (or honeycomb layers as mentioned above), is populated by Ga^{3+} and Cu^{2+} ions with 57% Ga^{3+} and 43% Cu^{2+} , see Fig. 6. The goodness of fit parameters R_p , R_{wp} , R_{exp} and χ^2 are found to be 2.67%, 2.94%, 0.34% and 75, respectively.

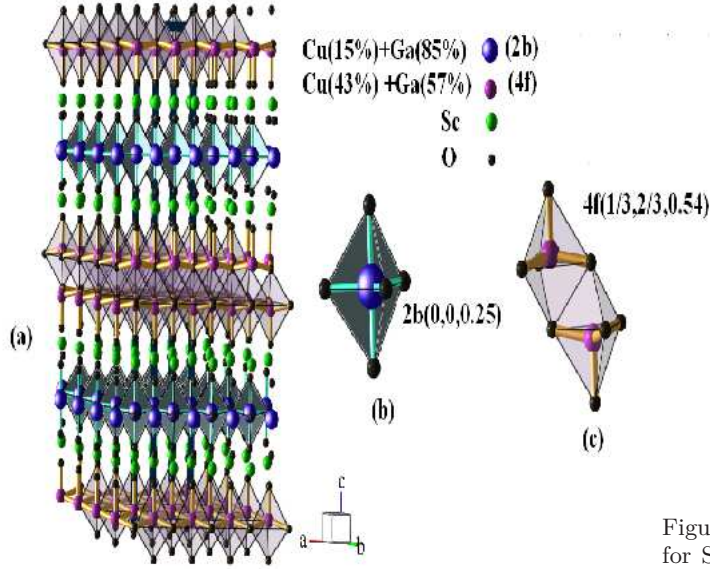


Figure 6: (Color online). (a) Local arrangement of atoms in a unit cell of SGCO is shown. Blue and magenta color balls each correspond to a fractional occupation by the Cu and Ga atoms as mentioned in the legend. Figures 1 (b) and 1 (c) represent the Cu/Ga environments at the 2b (corner-sharing triangular bipyramids) and the 4f (double layers of triangular bipyramids) sites, respectively.

Table II: Crystal structure parameters of SGCO as refined from synchrotron data ($\lambda = 1.38455$ Å) at 300 K with space group $P6_3/mmc$. The occupancies of Cu and Ga at both sites have been constrained to ensure the ratio of total amounts of Cu and Ga to be 1:2.

Atom	site	x	y	z	occupancy
Sc	4f	1/3	2/3	0.14865(2)	1
Cu1/Ga1	2b	0	0	1/4	0.15(1)/0.85(1)
Cu2/Ga2	4f	1/3	2/3	0.54480(1)	0.43(1)/0.57(1)
O1	4f	0	0	0.17934(7)	1
O2	4f	1/3	2/3	0.61118(7)	1
O3	4f	1/3	2/3	0.03371(7)	1
O4	2c	1/3	2/3	1/4	1

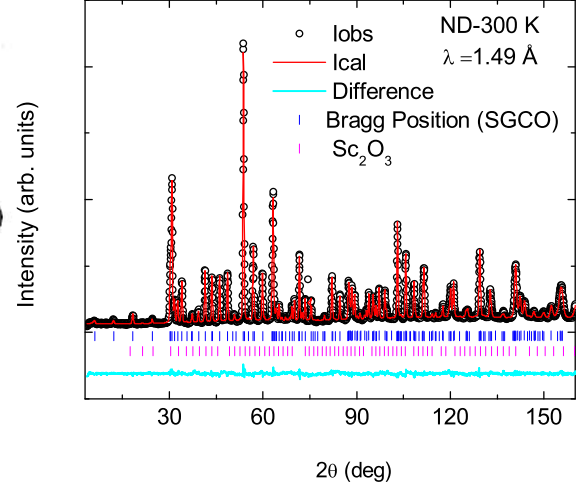


Figure 7: (Color online) Neutron diffraction data measured for SGCO with $\lambda = 1.49$ Å at 300 K are shown. The open black circles and the red solid line represent the experimental and refined data. The vertical blue and pink lines indicate the Bragg positions for SGCO and Sc_2O_3 , while flat cyan line shows the difference plot between measured and refined intensities.

Table III: Refined positional parameters and the occupancies for SGCO at 300 K under the space group $P6_3/mmc$ using the neutron diffraction data with $\lambda = 1.49$ Å.

Atom	Wyckoff position	x	y	z	Occupancy
Sc	4f	1/3	2/3	0.14861(5)	0.93
Cu	2b	0	0	1/4	0.66
Ga	2b	0	0	1/4	0.34
Cu	4f	1/3	2/3	0.54447(5)	0.16
Ga	4f	1/3	2/3	0.54447(5)	0.84
O1	4f	0	0	0.18087(7)	1
O2	4f	1/3	2/3	0.61201(6)	1
O3	4f	1/3	2/3	0.03320(10)	1
O4	2c	1/3	2/3	1/4	1

Similarly, the neutron diffraction measurements performed at 300 K, shown in Fig. 7, also could not reliably infer the amount of site sharing between Cu^{2+} and Ga^{3+} ions, because of a poor contrast between their scattering lengths, 7.718 and 7.288 fm, respectively [1]. Consequently, based on our neutron diffraction data alone we could not have made a definitive statement about the site occupancy by Ga and Cu at the 2b and 4f sites. The obtained lattice constants from neutron diffraction data ($\lambda = 1.49$ Å) are $a = b = 3.30459(4)$ Å and $c = 28.1183(4)$ Å, in good agreement with those obtained from x-ray (synchrotron) data. The residual refinement factors R_p , R_{exp} , R_{wp} and χ^2 for neutron refined powder diffraction pattern for 300K data yield 3.61%, 3.00%, 4.73% and 2.49, respectively. The refined atomic coordinates for

SGCO at 300 K are listed in the Table III. As it is evident from the refinement result that the neutron diffraction suggests a distribution of Cu and Ga quite opposite to what was determined from resonant x-ray data. The neutron diffraction data collected at 1.5 K (Fig. 8) do not show the appearance of any new peak and hence rule out the presence of magnetic ordering.

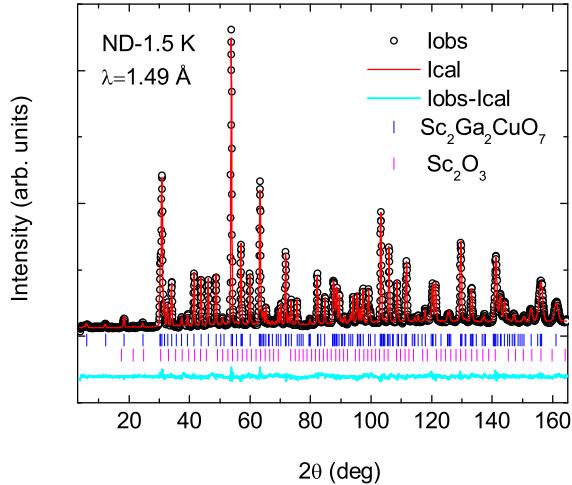


Figure 8: (Color online) Neutron diffraction data for SGCO, collected at 1.5 K, with its Rietveld refinement is shown. Vertical blue and pink bars depict the Bragg positions for SGCO (main phase) and Sc_2O_3 (impurity phase $\sim 1.2\%$).

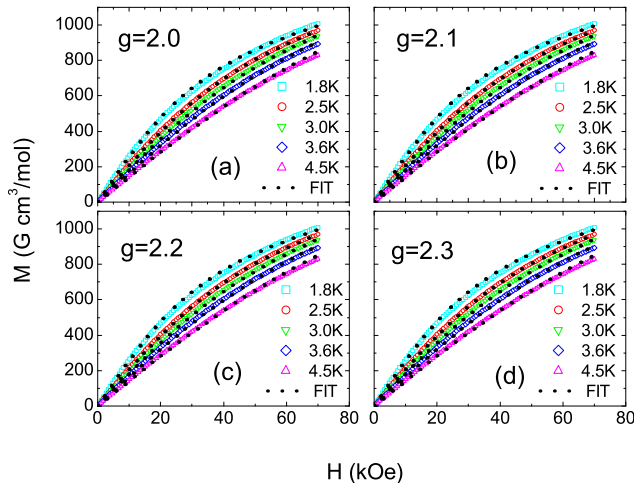


Figure 9: (Color online) The magnetization isotherms measured in the field range (0-70 kOe) and in the temperature range 1.8-4.5 K are shown. The dotted broken lines are fits to an equation described in the text. The panels (a), (b), (c), and (d) illustrate these fits for various values of the spectroscopic splitting factor $g = 2.0, 2.1, 2.2$, and 2.3 , respectively.

C. Magnetization isotherm analysis

As it is evident from Fig. 9, below about 5 K magnetization isotherms start to show a curvature, which becomes prominent at lower temperatures. Measured magnetic isotherms in the temperature range 1.8-4.5 K, where $\mu_B H$ is no longer much smaller than $k_B T$, were analyzed within the framework of the following equation: $M(H, T) = \chi(T)H + N_A \mu_B f_{imp} S_{imp} g_{imp} B_S(g_{imp} S_{imp} H \mu_B / k_B (T - \theta_{imp}))$, where χ represents the intrinsic susceptibility of the triangular planes and is assumed constant in the 1.8-4.5 K interval, f_{imp} , g_{imp} , S_{imp} , and θ_{imp} denote the impurity/disorder concentration, the Lande g -factor, spin, and correlation temperature for impurity spins. The symbols H , N_A , k_B , μ_B , and B_S refer to the magnetic field, the Avogadro number, the Boltzmann constant, the Bohr magneton, and the Brillouin function, respectively. To start with, there are five-parameters to be varied and a simultaneous fitting of all these end up in nonphysical values. So we first fixed S_{imp} and g_{imp} to be 1/2 and 2, respectively and thus reduced our variables from five to three, *i.e.*, χ , f_{imp} and θ_{imp} . To increase the reliability of our fitting parameters we simultaneously fitted all magnetic isotherms, measured in the T -range 1.8 - 4.5 K. The outcomes of fittings for various assumed values of g are summarized in Table. IV. As is evident from the result, the value of θ_{imp} is nearly zero, which in turn suggests the absence of magnetic correlations among impurity spins so one can treat them as purely paramagnetic. The obtained free-spin concentration is consistent with about 12% antisite disorder.

Table IV: Results of various fits to the magnetization isotherm data with the equation described in text.

S_{imp}	g_{imp}	$\chi(\text{cm}^3/\text{mol})$	$\theta_{imp}(\text{K})$	$f_{imp}(\%)$
1/2	2.0	0.0051	-0.22	11.60
1/2	2.1	0.0047	-0.42	11.58
1/2	2.2	0.0043	-0.63	11.59
1/2	2.3	0.0038	-0.85	11.61

D. A.C. susceptibility

AC susceptibility data were measured in the temperature range 0.3 - 7 K and 2- 30 K on a home-made susceptometer and a Quantum Design SQUID VSM machine, respectively. The data were recorded keeping the dc field zero and the ac pulse of amplitude 5 Oe. With the home-made susceptometer we measured the data for three different frequencies of 545.7 Hz, 311 Hz, and 155 Hz. In the temperature range 2-30 K on Quantum design SQUID VSM machine we measured the data for five different frequencies of 11 Hz, 110 Hz, 155 Hz, 311 Hz, and 546

Hz. The data obtained with the home made susceptometer were multiplied by a scaling factor (after subtracting a background) so as to match the data between 2 K and 7 K obtained using the Quantum Design SQUID VSM. The real part of the susceptibility data is shown in Fig. 10. These data do not show any frequency dependence or any peak in the entire measured temperature range and thus rule out the possibility of any glassy behavior in this material within the precision of our measurements.

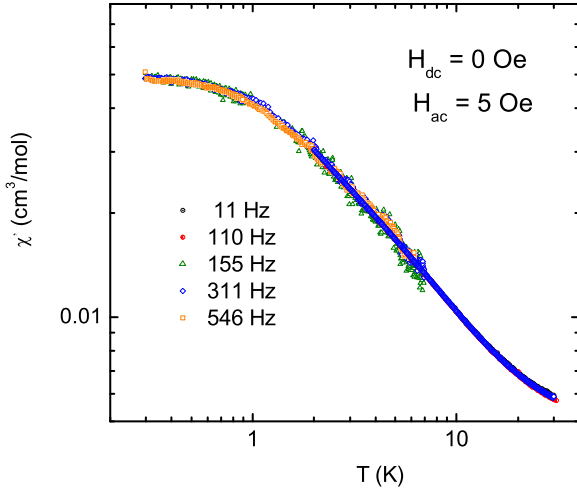


Figure 10: Variation of the real part of the ac susceptibility as a function of temperature (0.3-30 K) for several frequencies is shown.

E. Magnetic specific heat analysis

The $C_p(T)$ data, specific heat at constant pressure, data obtained in zero magnetic field in the temperature range 0.35-300 K are shown in Fig. 11. The total specific heat of the system can be written as: $C_p(T) = C_{lattice} + C_{Schottky} + C_m$. Here, $C_{lattice}$ is the lattice specific heat and $C_{Schottky}$ originates from isolated paramagnetic spins (Cu^{2+} spins in this case) forming a two-level system. We ascribe the remaining contribution C_m to antiferromagnetically interacting Cu^{2+} spins residing in the 4f planes (bi-planes). We now attempt to estimate $C_{lattice}$ and $C_{Schottky}$ so that the "intrinsic" contribution C_m can be inferred.

To estimate the lattice contribution ($C_{lattice}$) in the absence of a suitable non-magnetic analog for SGCO, we used a combination of Debye and Einstein terms, as written in Eqn. (1) given below.

$$C_{lattice}(T) = C_{Debye} + C_{Einstein} \quad (1)$$

$$\text{where, } C_{Debye} = C_D \left[9k_B \left(\frac{T}{\theta_D} \right)^3 \int_0^{\frac{x_D}{T}} \frac{x^4 e^x}{(e^x - 1)^2} dx \right] \text{ and}$$

$$C_{Einstein} = \sum C_{E_i} \left[3R \left(\frac{\theta_{E_i}}{T} \right)^2 \frac{\exp(\frac{\theta_{E_i}}{T})}{\left(\exp(\frac{\theta_{E_i}}{T}) - 1 \right)^2} \right]$$

One formula unit of SGCO has twelve atoms and this in turn offers one acoustic and eleven optical modes of atomic vibrations, in each crystallographic direction. The first term (Debye integral) of the Eqn. (1) takes care of the three acoustic modes of vibration whereas the second term accounts for the contribution of thirty three optical modes of phonons. This amounts to the conditions $C_D = 1$ and $\sum C_{E_i} = 11$ or $C_D + \sum C_{E_i} = 12$ for each direction. The data were found to fit well with weightage factors corresponding to Debye and Einstein modes chosen in the ratio 1:1:4:6. We, however, understand that this is just a simple model to capture the basic characteristics of the complex lattice dynamics. We initially fitted the $C_p(T)$ data to Eqn. (1) in the temperature range 20-90 K and then extrapolated the curve to cover the entire temperature range 0.35-300 K, as shown in the inset (a) of Fig. 11. The fitting yields the Debye temperature to be 159 K and Einstein temperatures to be 231 K, 308 K and 645 K, respectively. Nevertheless, at very low temperatures ($T \ll \theta_D$: Debye temperature) only the first term (acoustic branch of the phonon spectrum) dominates as T^3 and Einstein weightage to the lattice specific heat falls rapidly as $\exp(-\theta_D/T)$.

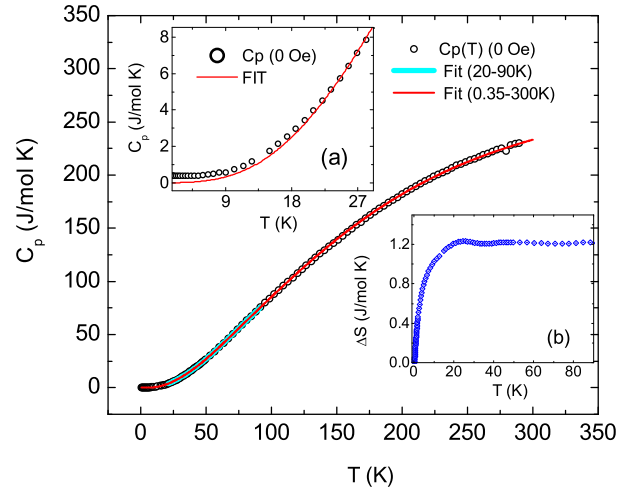


Figure 11: (Color online) Heat capacity at zero field is shown with black open circles. Cyan and red solid lines represent initial fit (20-90 K) to a combination of Debye and Einstein model and its extrapolation in the entire temperature range (0.35-300 K), respectively. Inset (a) highlights the low-temperature portion of the $C_p(T)$ data and inset (b) illustrates the entropy change at zero field.

Next, we will estimate the Schottky contribution $C_{Schottky}$ as follows. Based on magnetization isotherm analysis, we modeled the Schottky contribution ($C_{Schottky}$) by fixing the amount of free spins to 12%. We

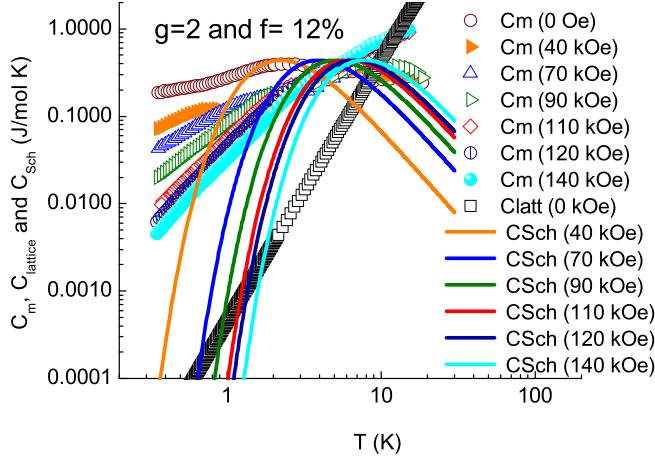


Figure 12: (Color online) Individual contributions of lattice $C_{lattice}$ (open squares), Schottky $C_{Schottky}$ (various solid lines as per field for $f=12\%$) and magnetic specific heats C_m (other open and closed symbols) to the total specific heat are shown in the field range 0-140 kOe.

used the two-level Schottky formula, described by Eqn. 2 below, with $f = 12\%$ contribution from non-interacting Cu-spins having a g -value of 2.

$$C_{Schottky} = f \left[R \left(\frac{\Delta}{k_B T} \right)^2 \left(\frac{g_0}{g_1} \right) \frac{\exp(\frac{\Delta}{k_B T})}{[1 + (\frac{g_0}{g_1}) \exp(\frac{\Delta}{k_B T})]^2} \right] \quad (2)$$

Here, Δ is the energy separation under the influence of an external magnetic field H , and R , k_B , g_0 and g_1 are the universal gas constant, the Boltzmann constant, and the degeneracies of the two level system, respectively.

The "intrinsic" magnetic specific heat C_m is thus obtained by subtracting $C_{lattice} + C_{Schottky}$ from $C_p(T)$.

Figure 12 illustrates a plot of individual contributions of Schottky (for $g = 2$ and 12% free spin contribution), lattice and magnetic specific heats to the total specific heat data. It is worth mentioning that below about 1 K the lattice heat capacity as also the Schottky contribution in fields beyond 90 kOe is utterly negligible in the total specific heat and the determination of the magnetic specific heat (C_m) below 1 K is free from any uncertainty. Further, analyzing the magnetic heat capacity data assuming a $\pm 50\%$ uncertainty in the Schottky part does not change significantly the values of exponents for fields $H > 40$ kOe, and the exponents are found to be robust for $H > 40$ kOe (see main text and Fig. 4 (c)). Note that Fig. 13 shows the lattice removed $C_p(T)$ data, a sum of both the magnetic and Schottky specific heat, for SGO at different magnetic fields.

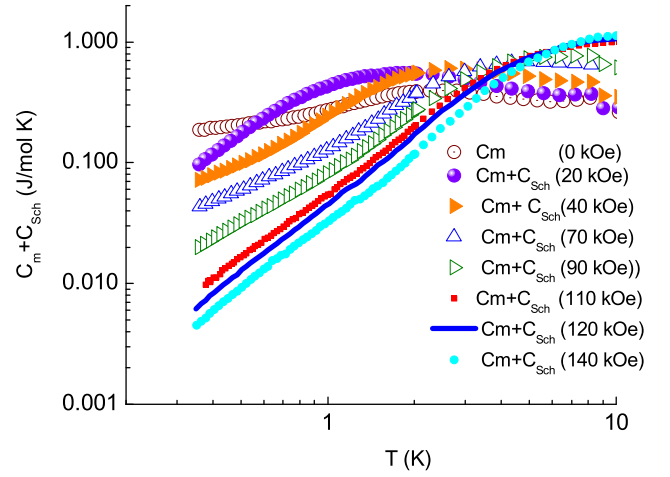


Figure 13: (Color online) A sum of magnetic specific heat C_m and Schottky specific heat $C_{Schottky}$ is shown for fields 0 - 140 kOe as a function of temperature.

[1] See for neutron scattering lengths: <http://www.ncnr.nist.gov/resources/n-lengths/>